

# Trigonometric Functions Study Guide

## SINE FUNCTIONS

Standard Form:  $y = a \sin(bx - c) + d$

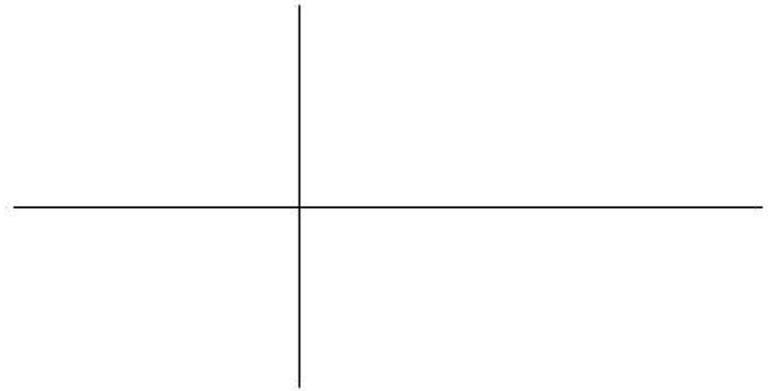
**Amplitude:**

**Period:**

**Phase Shift:**

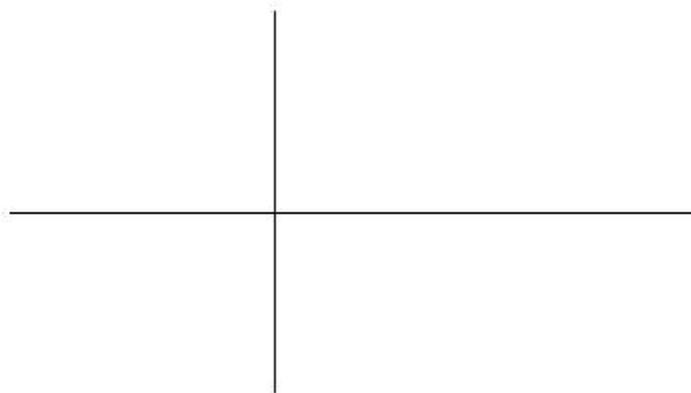
**Initial Interval:**

Parent Function  $y = \sin x$



### Practice Problems

$$y = 2 \sin\left(x - \frac{\pi}{4}\right)$$



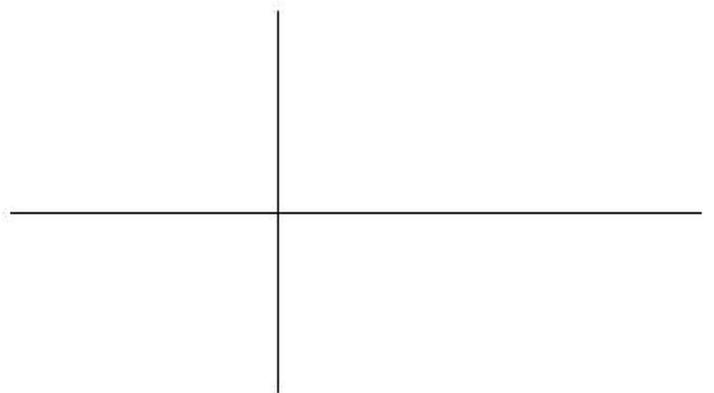
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = \sin(3x - \pi)$$



**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = -3 \sin(2x)$$



**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = \sin(x - \pi) + 3$$



**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = 2 \sin\left(\frac{x}{3} + \frac{\pi}{3}\right)$$



**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

## COSINE FUNCTIONS

**Standard Form:**  $y = a \cos(bx - c) + d$

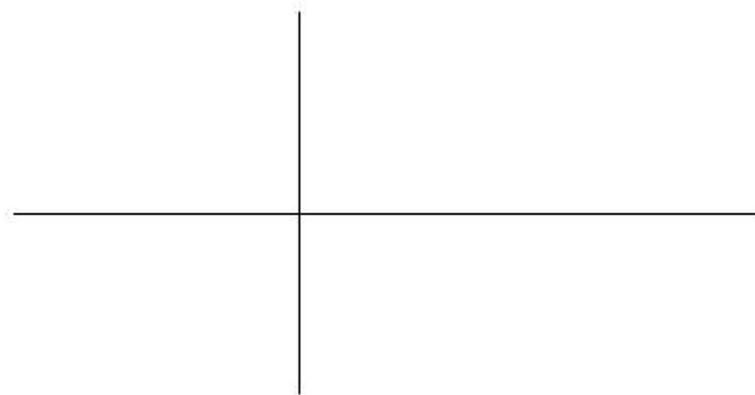
**Amplitude:**

**Period:**

**Phase Shift:**

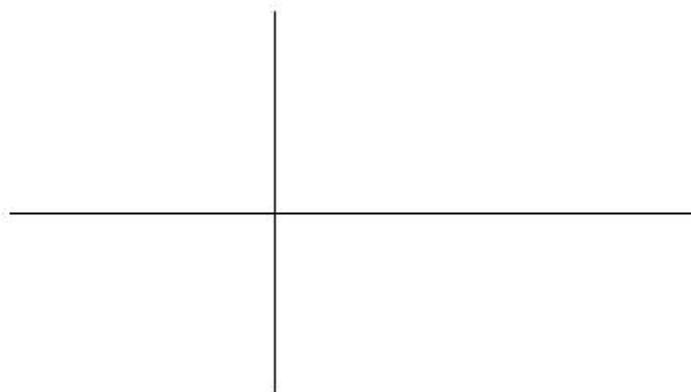
**Initial Interval:**

**Parent Function**  $y = \cos x$



Practice Problems

$$y = 3 \cos\left(x - \frac{\pi}{2}\right)$$



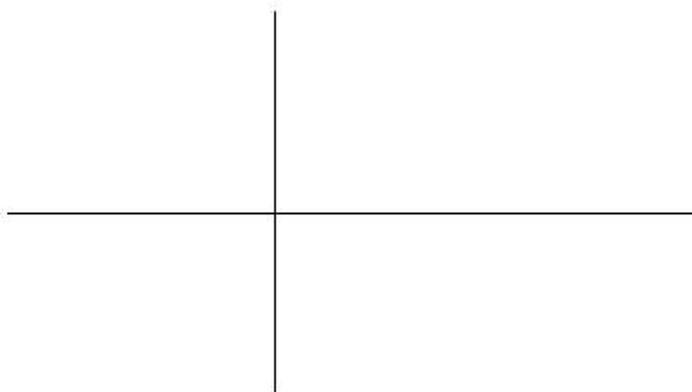
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = -2 \cos\left(\frac{x}{4} - \frac{\pi}{3}\right)$$



**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = \cos(\pi x) + 1$$



**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = -\cos(2x - \pi) - 2$$



**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = \cos\left(\frac{x}{2} + \frac{\pi}{3}\right)$$



**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

## COSECANT FUNCTIONS

**Standard Form:**  $y = a \csc(bx - c) + d$

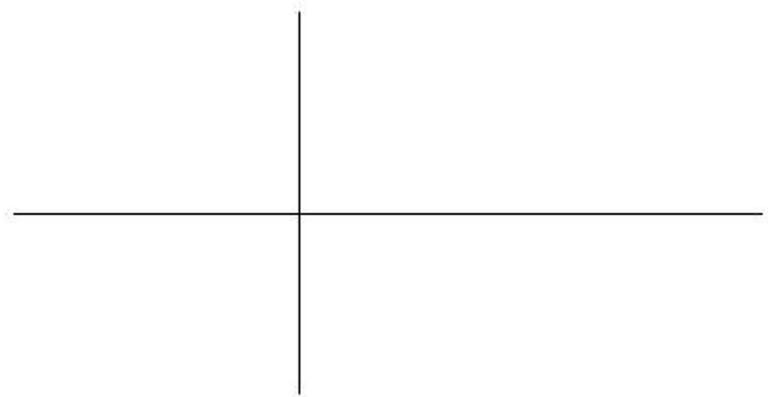
**Amplitude:**

**Period:**

**Phase Shift:**

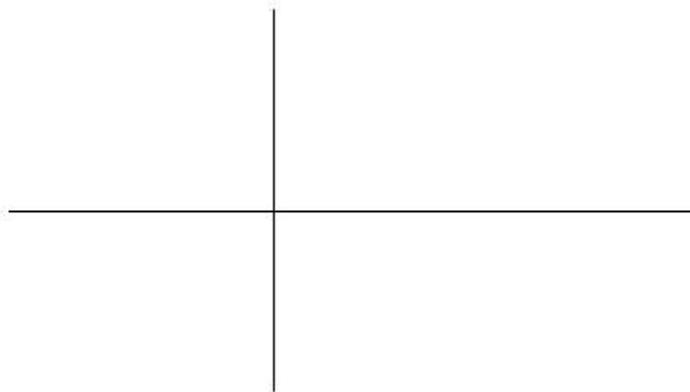
**Initial Interval:**

**Parent Function**  $y = \csc x$



Practice Problems

$$y = \csc\left(\frac{x}{2} - \pi\right)$$



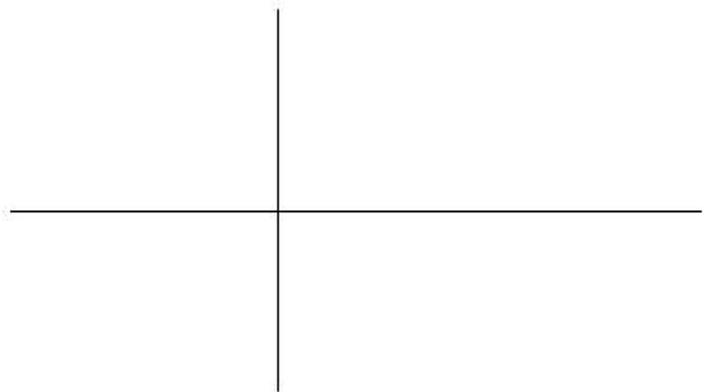
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = -\csc\left(3x - \frac{\pi}{4}\right)$$



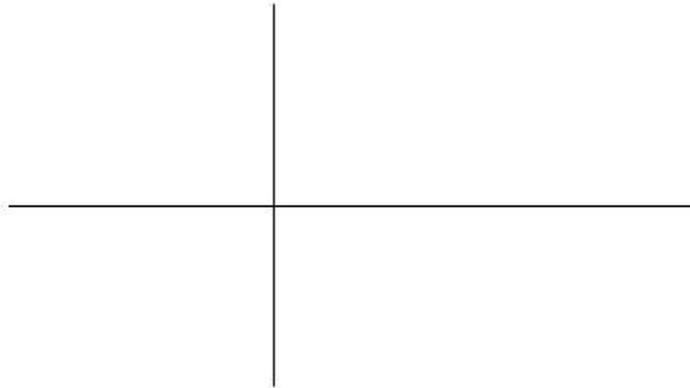
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = 2 \csc(\pi - 2x)$$



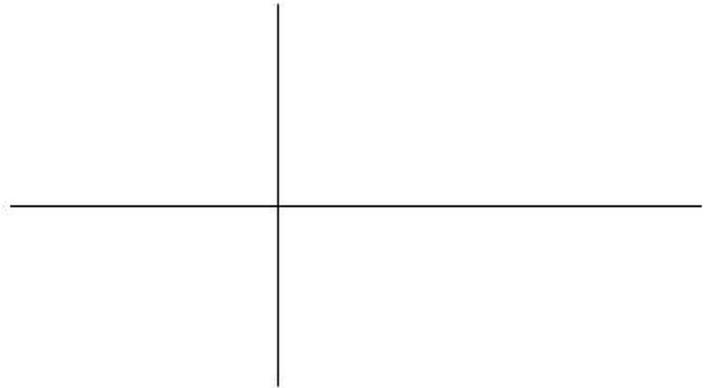
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = -\csc\left(x + \frac{\pi}{4}\right) + 1$$



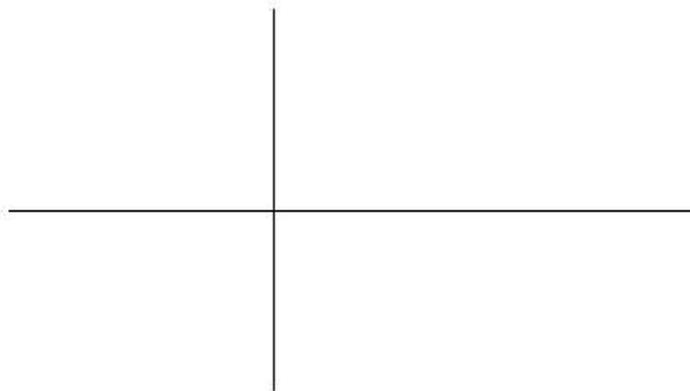
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = \csc\left(\frac{2x}{3}\right)$$



**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

## SECANT FUNCTIONS

**Standard Form:**  $y = a \sec(bx - c) + d$

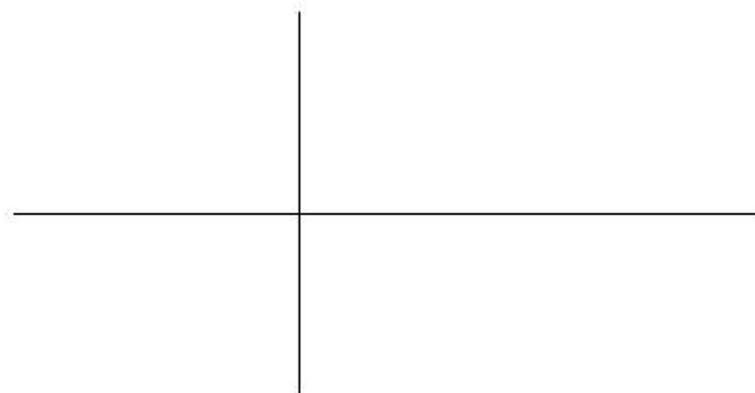
**Amplitude:**

**Period:**

**Phase Shift:**

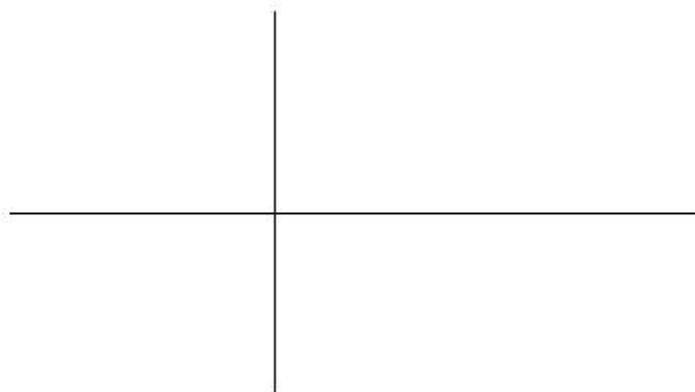
**Initial Interval:**

**Parent Function**  $y = \sec x$



Practice Problems

$$y = \sec(3x - \pi)$$



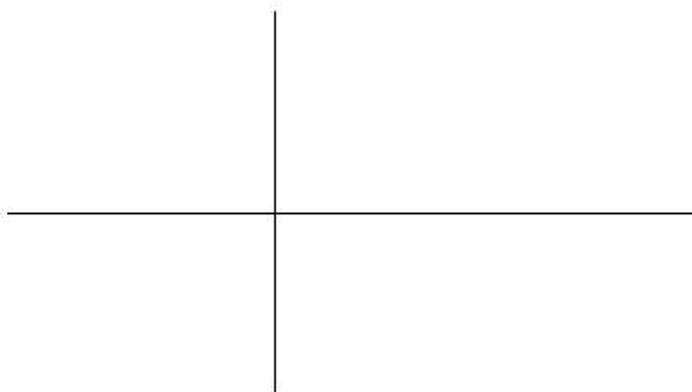
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = -2 \sec\left(x - \frac{\pi}{3}\right)$$



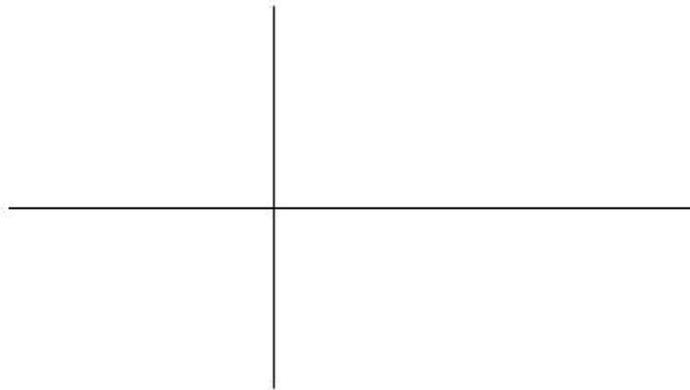
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = 3 \sec\left(x + \frac{\pi}{6}\right)$$



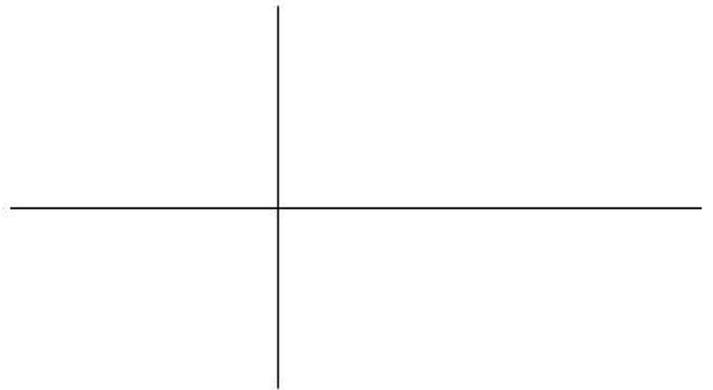
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = -2 \sec\left(3x - \frac{\pi}{2}\right) + 1$$



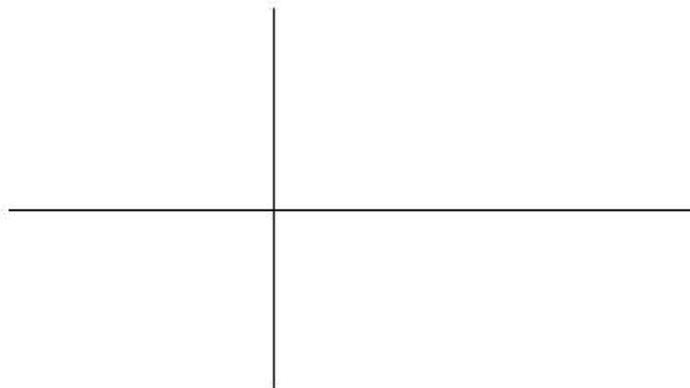
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = \sec(2\pi x)$$



**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

## TANGENT FUNCTIONS

**Standard Form:**  $y = a \tan(bx - c) + d$

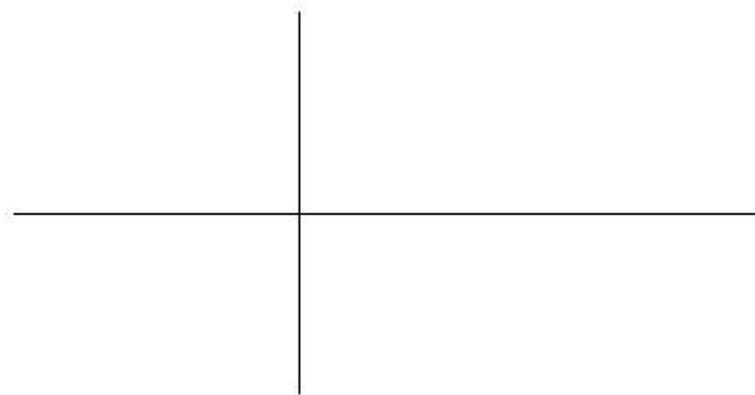
**Amplitude:**

**Period:**

**Phase Shift:**

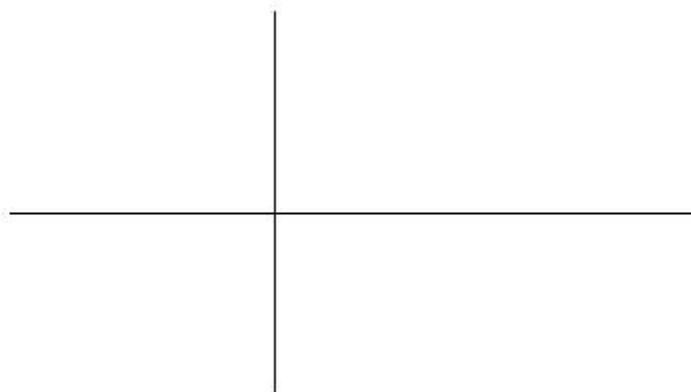
**Initial Interval:**

**Parent Function**  $y = \tan x$



Practice Problems

$$y = \tan\left(\frac{x}{3}\right)$$



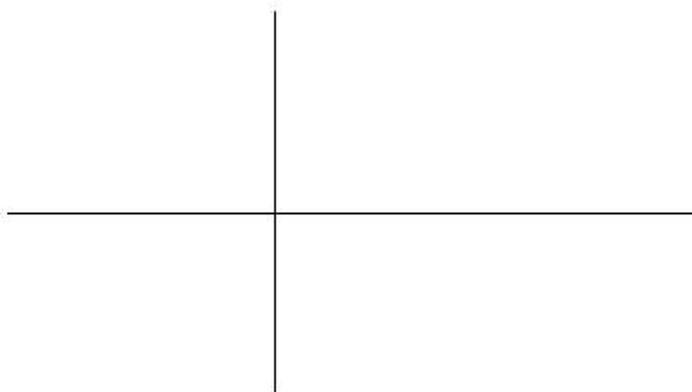
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = \tan\left(2x - \frac{\pi}{2}\right)$$



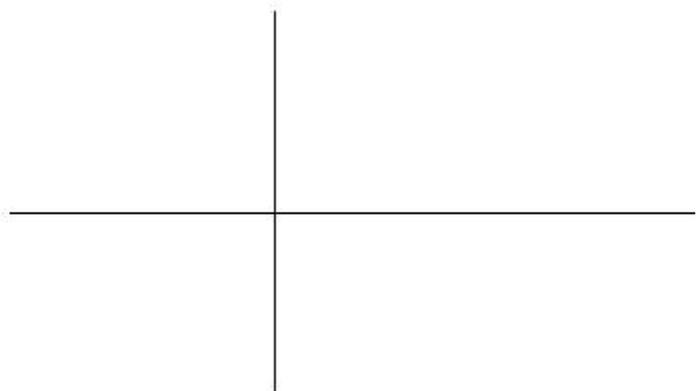
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = -2 \tan(x + \pi)$$



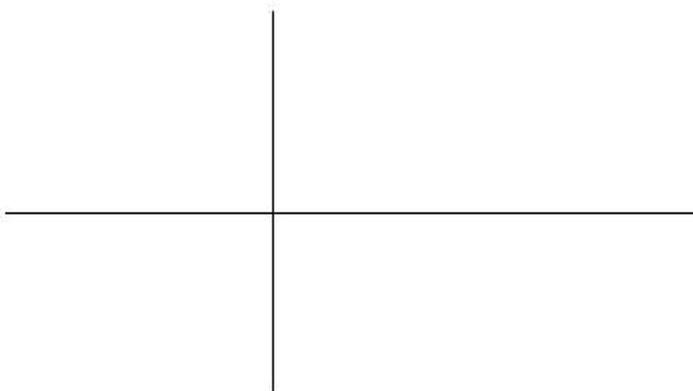
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = -\tan\left(\frac{3x}{2}\right)$$



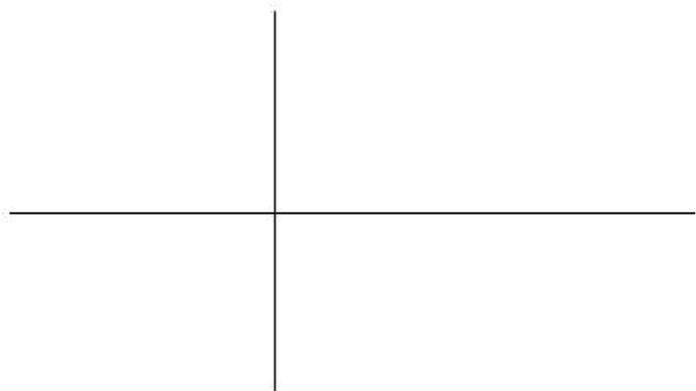
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = \tan(x + \pi)$$



**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

## COTANGENT FUNCTIONS

**Standard Form:**  $y = a \cot(bx - c) + d$

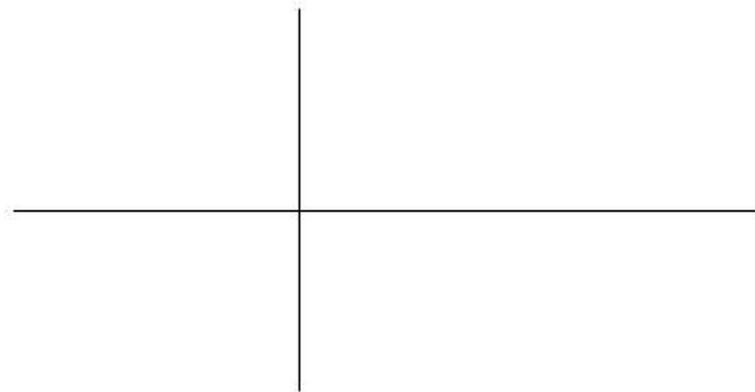
**Amplitude:**

**Period:**

**Phase Shift:**

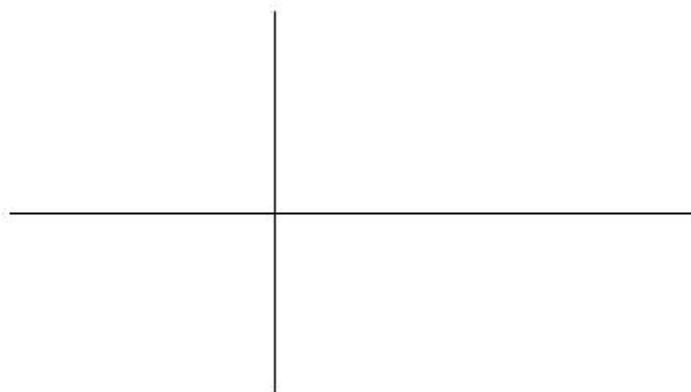
**Initial Interval:**

**Parent Function**  $y = \cot x$



Practice Problems

$$y = \cot\left(\frac{x}{3}\right)$$



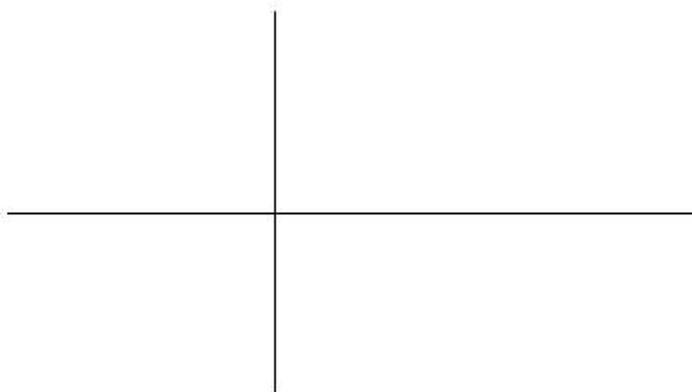
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = \cot\left(\pi x - \frac{\pi}{2}\right)$$



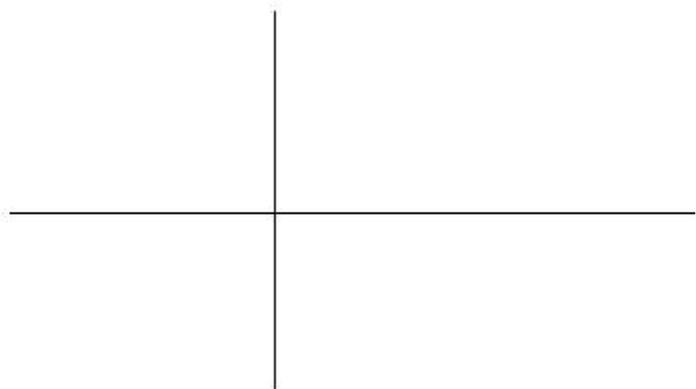
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = \cot\left(x - \frac{\pi}{2}\right)$$



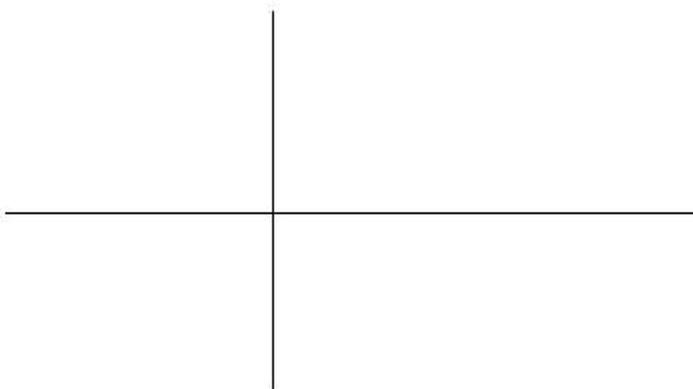
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = \cot\left(\frac{3x}{2} - \pi\right)$$



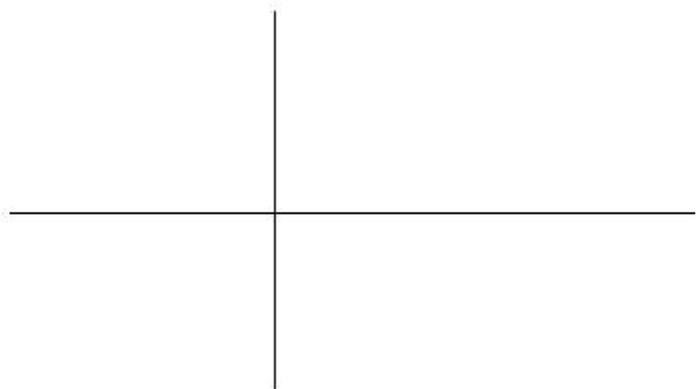
**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**

$$y = -\cot(2x + \pi)$$



**Amplitude:**

**Period:**

**Phase Shift:**

**Initial Interval:**