

LOGARITHMS

Logarithmic Form

$$\log_a b = c$$

Exponential Form

$$a^c = b$$

Read a logarithm as: "log base a of b is c."

$$\log_4 16 = 2$$

The question you are answering is: "To what power do I raise 4 to get 16?"

Evaluate

$$\log_6 36 =$$

$$\log_8 2 =$$

$$\log_3 \frac{1}{27} =$$

$$\log_4 8 =$$

$$\log 1000 =$$

$$\log_3 -9 =$$

$$\log_{32} 64 =$$

$$\log_7 7^{5.23} =$$

$$\log_{16} \frac{1}{2} =$$

The value of $\log_3 56$ lies between which two consecutive integers?

- A) 1 and 2
- B) 2 and 3
- C) 3 and 4
- D) 4 and 5

The value of $\log_2 \square$ lies between 4 and 5. Find the missing integer so that this statement is true.

Base Change Formula

$$\log_a b = \frac{\log b}{\log a}$$

Evaluate using a calculator:

$$\log_6 40 =$$

$$\log_3 19 =$$

Properties of Logarithms

- 1) $\log_a 1 = 0$ because $a^0 = 1$
- 2) $\log_a a = 1$ because $a^1 = a$
- 3) $\log_a a^x = x$ because $a^x = a^x$

Also the inverse property

$$a^{\log_a x} = x \quad \text{so} \quad 4^{\log_4 17} = 17$$

- 4) The one-to-one property

$$\text{If } \log_a x = \log_a y$$

$$\text{Then } x = y$$

Example of one-to-one property

$$\log_2 (x - 5) = \log_2 10$$

Solving logarithmic equations

Solve for x: $\log(5x + 3) = \log 12$

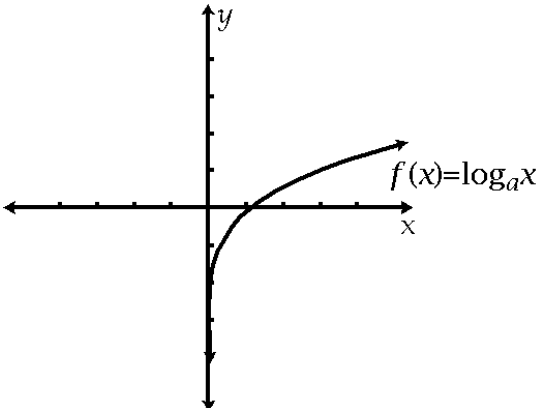
Solve for x: $\ln(x^2 - x) = \ln 6$

GRAPHING LOGARITHMIC FUNCTIONS

Standard Form: $y = a \log_n (bx - c) + d$

or

$y = a \ln (bx - c) + d$

<u>Vertical Asymptote</u>	<u>Domain</u>	<u>Parent Function</u>
<p>To find the V.A., set $bx-c=0$ and solve for x.</p> <p>V.A.: $x = \#$</p>	<p>To find the domain, set $bx-c>0$ and solve for x.</p> <p>Domain: $x > \#$</p>	

The Horizontal Axis (Not an Asymptote)

Given by: $y = d$

The Key Point

To find the x value of the key point, set $bx-c=1$ and solve for x . Then, substitute that value back into the equation to find the y value of the key point.

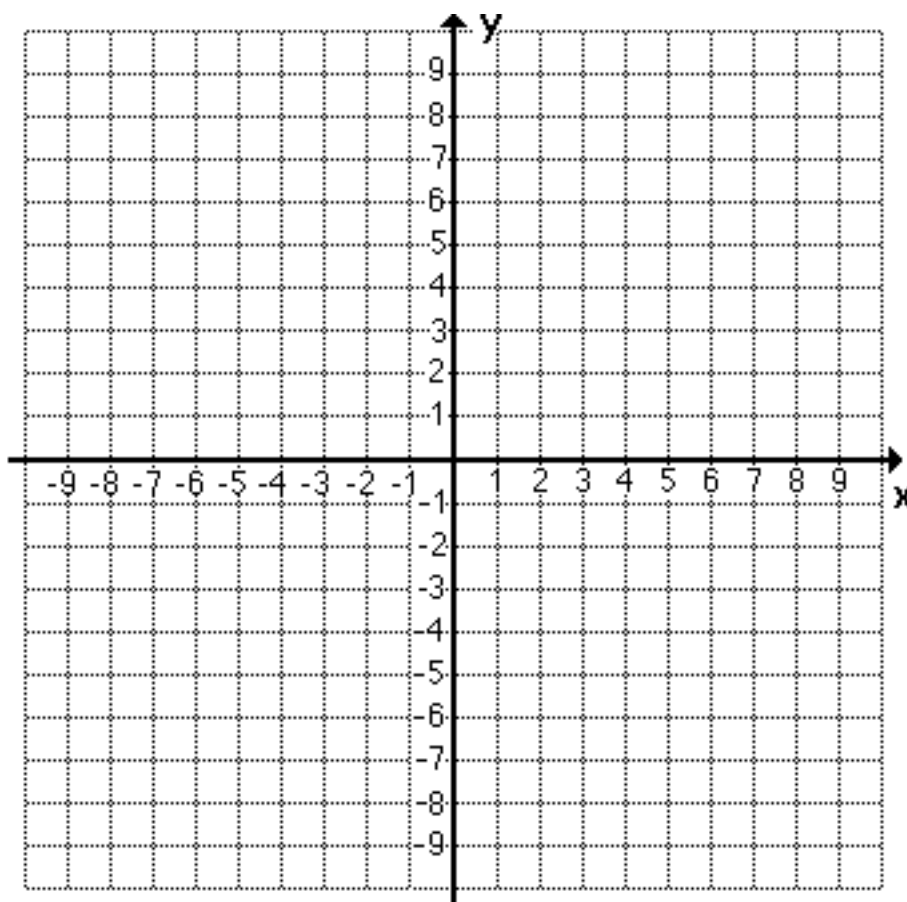
Example $y = 2 \log_3 (x + 4) - 6$

The Shape of the Curve

When graphing logarithmic functions, you will move in terms of powers of the base.

For example, if the problem you are graphing is $y = \log_3 x$ the movements, starting from the origin will be:

- Over 1, up 0.
- Over 3, up 1.
- Over 9, up 2.
- Over 27, up 3...etc.



When dealing with transformations, we will find a “new origin.”

Once we find the “new origin,” all our movements will begin from that point.

Always remember, logarithmic functions have a tail end. You must draw that section for the graph to be complete.

Here are a couple of examples of transformations and using powers of the base to get the right curve.

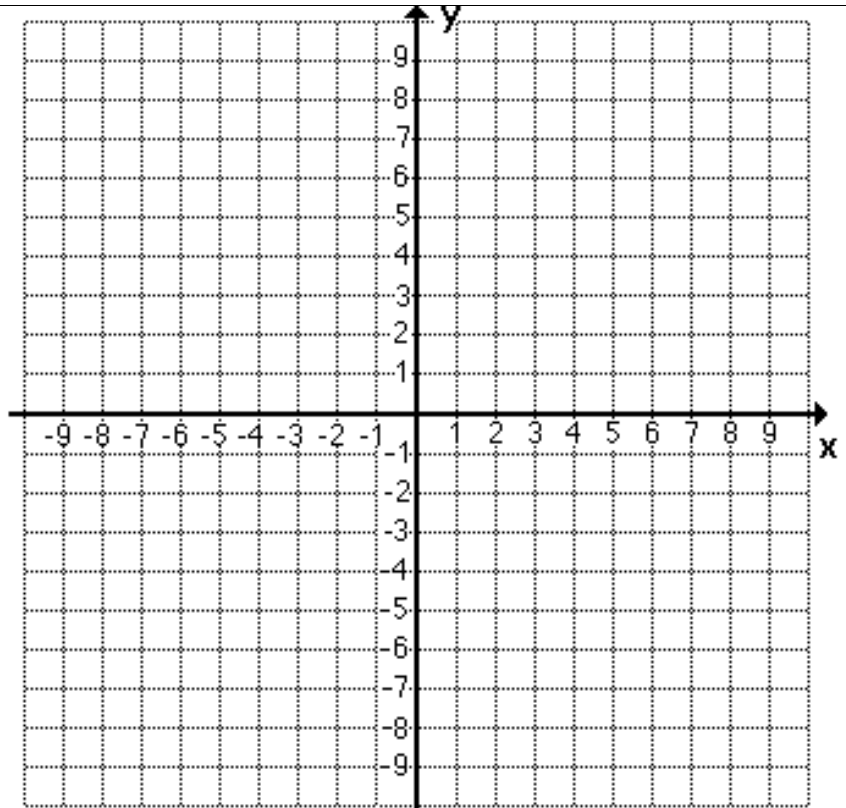
$$y = \log_2(x + 5) + 2$$

Vertical Asymptote:

Horizontal line of reference:

Movement

- Over 1, up 0.
- Over 2, up 1.
- Over 4, up 2.
- Over 8, up 3.
- Over 16, up 4.
- ...etc



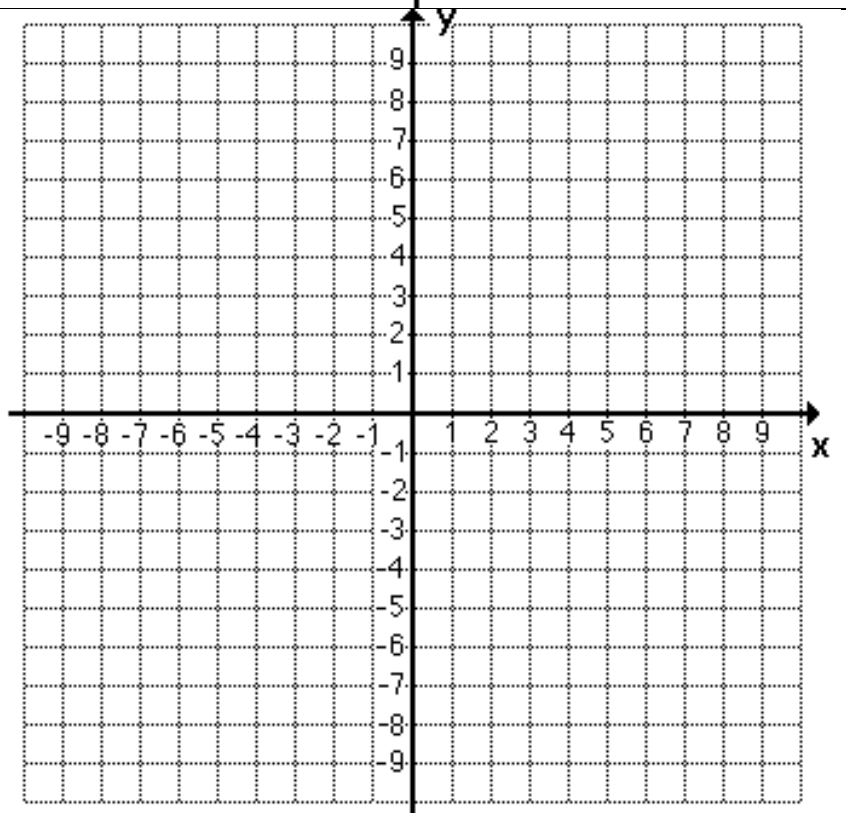
$$y = 3\log_2(x + 5) + 2$$

Vertical Asymptote:

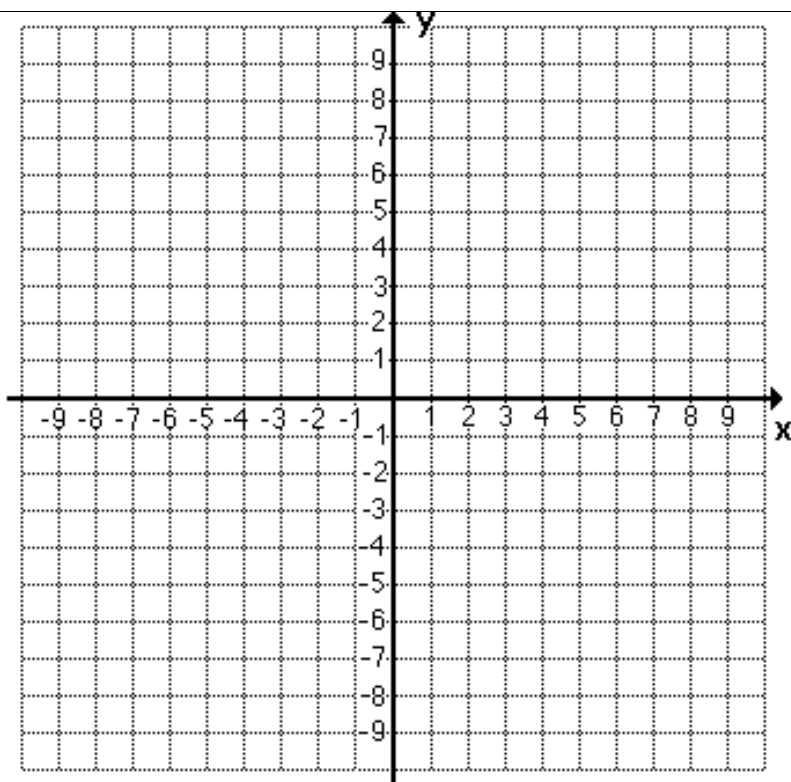
Horizontal line of reference:

Movement

- Over 1, up 0(3).
- Over 2, up 1(3).
- Over 4, up 2(3).
- Over 8, up 3(3).
- Over 16, up 4(3).
- ...etc



A) $f(x) = \log_2(x + 2)$



Key point:

Vertical Asymptote:

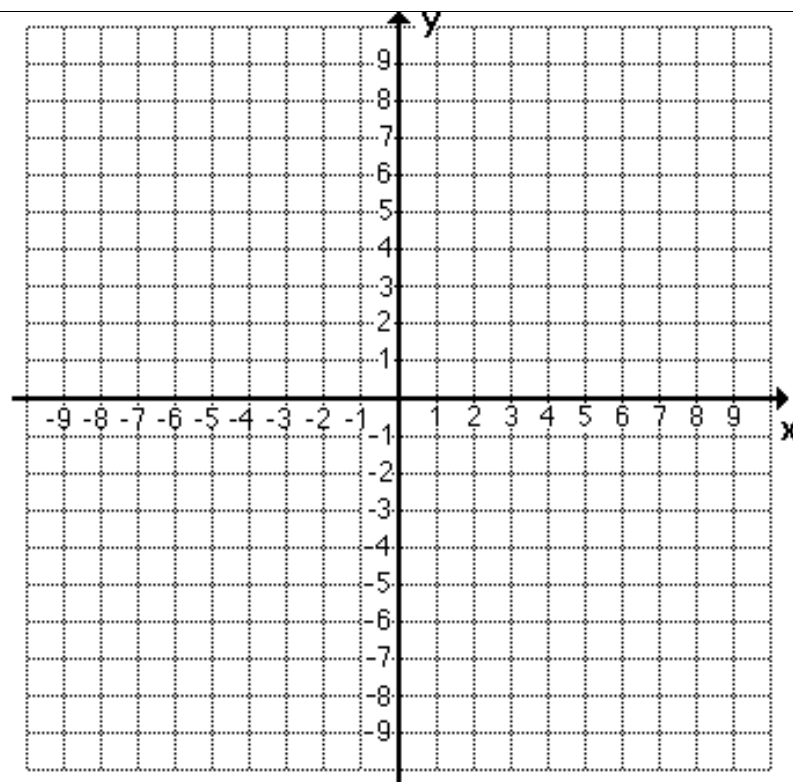
Y-intercept:

X-intercepts:

Domain:

Range:

B) $f(x) = \log_3(x - 1) + 2$



Key point:

Vertical Asymptote:

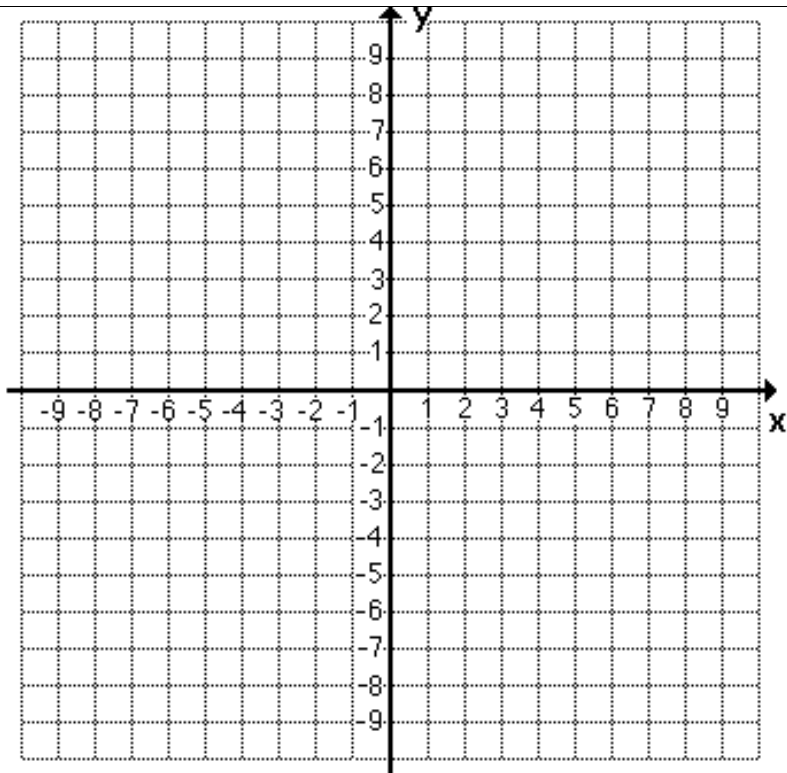
Y-intercept:

X-intercepts:

Domain:

Range:

c) $f(x) = \log_2(x+4) + 6$



Key point:

Vertical Asymptote:

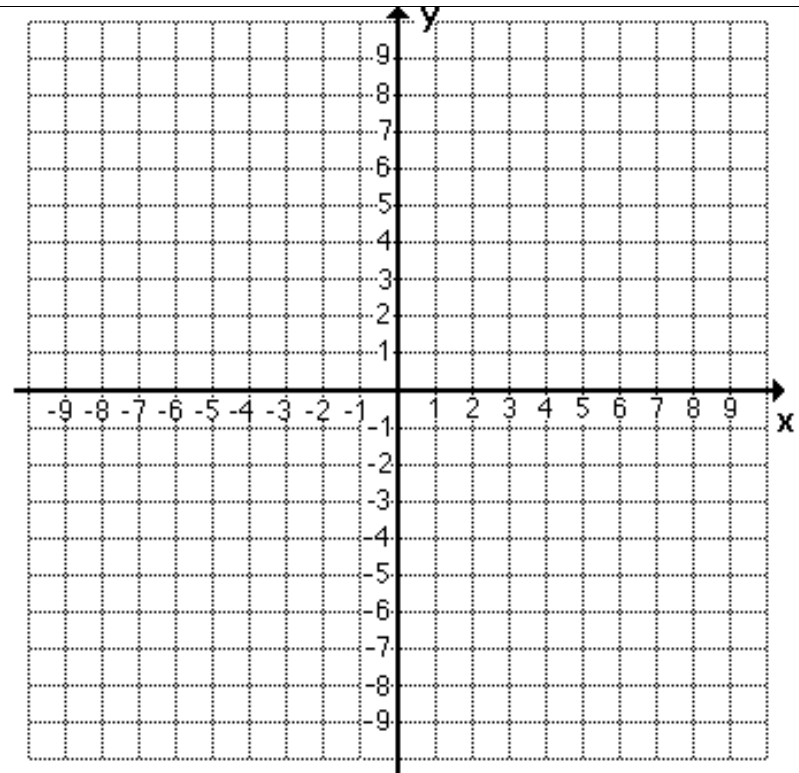
Y-intercept:

X-intercepts:

Domain:

Range:

D) $f(x) = 2\log_4(x+7) - 5$



Key point:

Vertical Asymptote:

Y-intercept:

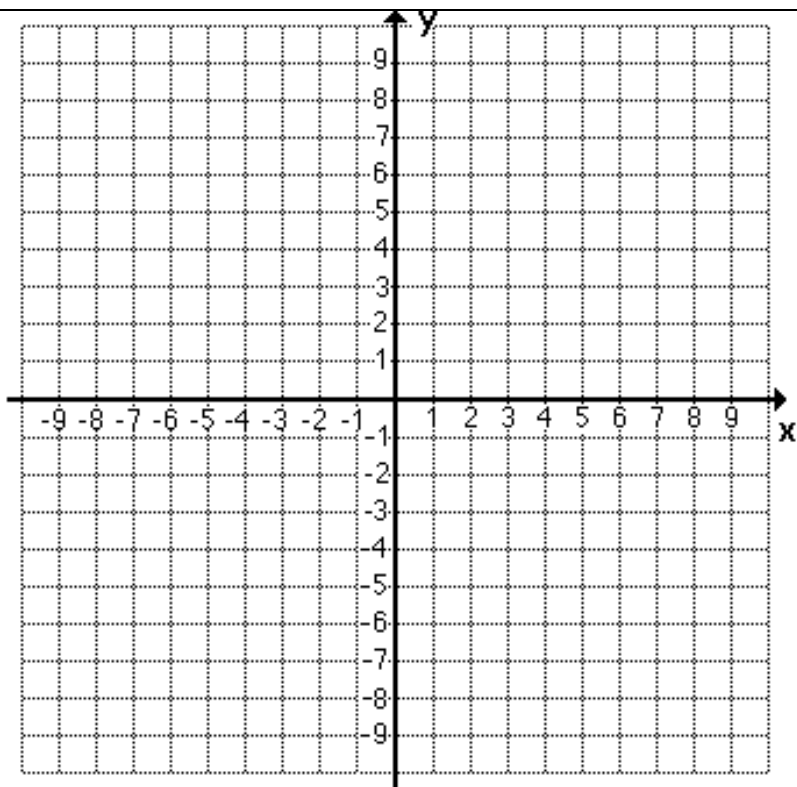
X-intercepts:

Domain:

Range:

E)

$$f(x) = -\ln(x-1) - 2$$



Key point:

Vertical Asymptote:

Y-intercept:

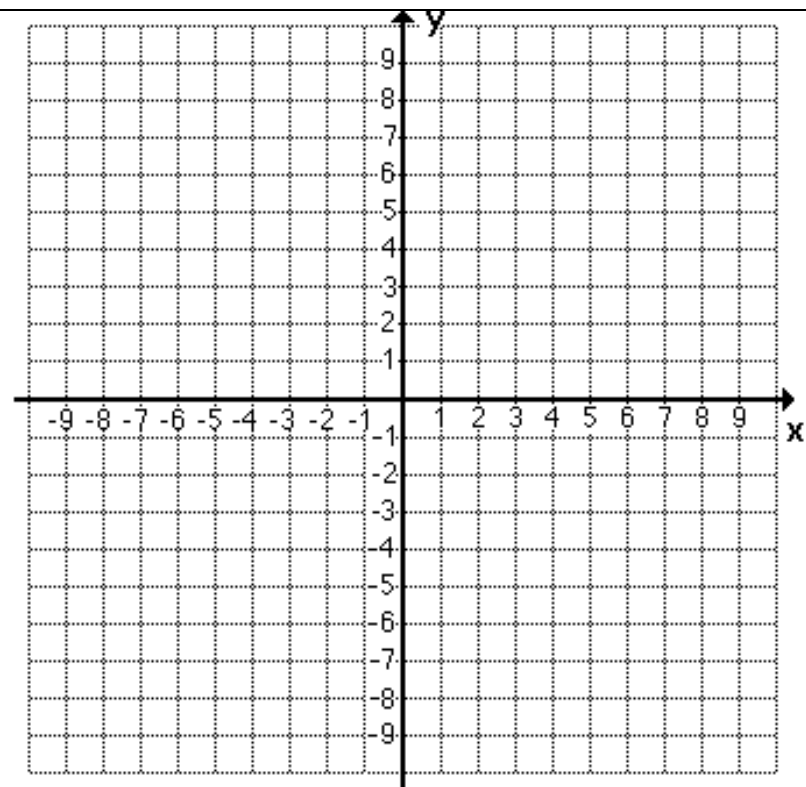
X-intercepts:

Domain:

Range:

F)

$$f(x) = 4 - \ln x$$



Key point:

Vertical Asymptote:

Y-intercept:

X-intercepts:

Domain:

Range:

